

Solving One-Step Equations

Date: 10-22-12

Objective: Today we will apply the properties of inverse operations in order to solve one-step linear equations.

Notes:

Equation: a mathematical statement that sets two expressions equal

Golden Rule of Algebra: whatever is done to one side of an equation must be done to the other to maintain equality

One-step equations can be solved by applying inverse operations

Inverse Operations: opposite operations that "undo" each other

What are examples of inverse operations?

Addition + Subtraction
Multiplication + Division
Fraction + Reciprocal

Example 1: Addition & Subtraction

$$\begin{array}{r} x - 2 = 5 \\ +2 \quad +2 \\ \hline x = 7 \end{array}$$

$$\begin{array}{r} x - 2 = 5 \\ 7 - 2 = 5 \checkmark \end{array}$$

Example 2: Addition & Subtraction

$$\begin{array}{r} n+8=4 \\ -8 \quad -8 \\ \hline n=-4 \end{array}$$

$$\begin{array}{r} n+8=4 \\ -4+8=4 \checkmark \end{array}$$

Example 3: Multiplication & Division

$$\begin{array}{r} -2x=3 \\ \frac{-2 \cdot x = 3}{-2 \quad -2} \\ 1x = \frac{3}{-2} \\ x = \frac{3}{-2} \end{array}$$

$$\begin{array}{r} -2 \cdot x = 3 \\ \frac{-2 \cdot 3}{1 \quad -2} = 3 \\ \frac{-6}{-2} = 3 \checkmark \end{array}$$

Example 4: Multiplication & Division

$$\frac{x}{-12} = 5$$

Handwritten work for Example 4: An arrow points from the 5 to the right, where it says $x \div -12 = 5$. Below this, a horizontal line is drawn with $\cdot 12$ on both sides, resulting in $x = -60$.

$$x = 5(-12)$$

$$x = -60$$

$$\frac{-60}{-12} = 5 \checkmark$$

Example 5: Multiplication & Division

$$-y = 15$$

$$-1y = 15$$

$$\frac{-1 \cdot y}{-1} = \frac{15}{-1}$$

$$y = -15$$

$$-1 \cdot (-15) = 15$$

$$15 = 15 \checkmark$$

Example 6: Fraction & Reciprocal

$$\frac{1}{2}x = -16$$

(Multiply)

$$\frac{1}{2} \cdot \frac{-32}{1} = -16$$

$$\text{reciprocal} = \frac{2}{1}$$

$$\sqrt{\frac{32}{2}} = -16$$

$$\frac{2}{1} \cdot \frac{1}{2}x = \frac{-16}{1} \cdot \frac{2}{1}$$

$$\frac{2}{2}x = \frac{-32}{1}$$

$$x = -32$$

Example 7: Fraction & Reciprocal

$$\frac{-5}{4}x = 55$$

$$\frac{-5 \cdot 44}{4 \cdot 1} = 55$$

$$\text{reciprocal} = \frac{4}{-5}$$

$$\frac{35}{1} = 55 \checkmark$$

$$\frac{4}{-5} \cdot \frac{-5}{4}x = \frac{55}{1} \cdot \frac{4}{-5}$$

$$\frac{-20}{-20}x = \frac{220}{-5}$$

$$x = -44$$

Exit Ticket

Solve for the unknown.

$$\textcircled{1} x - 4 = -16$$

$$\textcircled{2} 6x = -4$$

Check work!